

# **Calculation Policy for Mathematics**

The following calculation policy has been devised to meet requirements of the National Curriculum 2014 for the teaching and learning of mathematics, and is also designed to give pupils a consistent and smooth progression of learning in calculations across the school. Please note that early learning in number and calculation in Reception follows the "Development Matters" EYFS document, and this calculation policy is designed to build on progressively from the content and methods established in the Early Years Foundation Stage. The purpose of our Calculation Policy in setting out these aims is to ensure consistency in our approach to teaching calculation across the school. While compact methods may represent a significant achievement for some children it can present barriers for others. Each member of staff has a responsibility to ensure they give all children the opportunity to develop calculation methods that are appropriate to their age and ability.









### Age stage expectations

The calculation policy is organised according to age stage expectations as set out in the National Curriculum 2014. At Yarnfield Primary this includes; Stage 1 — Nursery and Reception

Stage 1 — Nursery and Recept Stage 2— Year 1 and 2 Stage 3— Year 3 and 4 Stage 4— Year 5 and 6



However, decisions about when to progress should always be based on the security of pupils' understanding and their readiness to broaden and deepen knowledge. Pupils who grasp concepts rapidly should be challenged through being offered rich and sophisticated problems before any acceleration through new content. Those who are not sufficiently fluent with earlier material should consolidate their understanding, including through additional practice, before moving on.

## Providing a context for calculation:

It is important that any type of calculation is given a real life context or problem solving approach to help build children's understanding of the purpose of calculation, and to help them recognise when to use certain operations and methods when faced with problems. This must be a priority within calculation lessons.

## Models & images and resources

At Yarnfield Primary staff must provide suitable resources for children to manipulate and explore how and why a calculation strategy works, and that helps them to describe and visualise or 'see' the method working. The equipment can include objects like counters, interlocking cubes, coins, counting sticks, bead strings, number lines, 100-squares, place-value cards, structural apparatus like base 10 blocks, tens frames, double-sided counters, Numicon, diagrams of shapes divided into fractional parts, and so on. An interactive whiteboard is also a powerful tool for manipulating images.

Selecting when and how to use and to withdraw resources and visual images is a key part of teaching. This involves planning how best to construct a blend of teaching approaches that are selected and designed to match intended learning outcomes and children's needs, and to take account of the context and organisation of children. Visualisation is important in mathematics. The ability to visualise representations, pictures or images and then adapt or change them is an important tool for example when problem solving, pattern spotting and reasoning in mathematics.

### **Problem Solving - Heuristics**

Providing pupils with opportunities to develop problem solving strategies is an essential part of teaching. By introducing the common heuristics to children, we will give them opportunities to 'see' and heuristic in operation and explore the strategy, helping them to become independent problem solvers.



- Simplify the problem
- Solve part of the problem

# **Calculation decision making**

Approximate

Making decisions about strategies to be used needs to be modelled by the classroom teacher, talking through the internal questions they are asking themselves as they calculate the question is essential. By involving children in this reasoning approach, through questioning them, will assist children to ask themselves similar questions whilst they are working.





# To work out a tricky calculation:

Calculate

Check it!

# Progression in mental and written computation.

Children use informal strategies in familiar settings e.g. touching dots, moving beads, making finger patterns. Begin to distance the setting from the child and pose problems involving 'bare numbers' for children to solve mentally. Children learn to combine mental strategies with informal written jottings for more difficult tasks. Using mental strategies and jottings we can develop semi-formal written strategies. If appropriate for the learner, we can develop these strategies further to formal written computational algorithms.



Mental strategies for addition and subtraction (written and pictorial (jottings) included for clarification – as they are taught strategies initially) Using labels for different strategies supports discussion about thinking and draws attention to the number relationships used. As a school we have chosen to prioritise 5 key methods that will be modelled for adding and subtracting mentally two 2digit numbers.



Begin from one number, jump tens then ones or ones and then tens E.g. 53 + 15





**Over-jump** Begin from one number, overshoot the jump and then compensate. To add or subtract 19, 18 or 17, jump 20, then back 1, 2, or 3. Over-jump is a form of compensation strategy, because it involves rounding one number to a decuple and then compensating. For example in solving 53 – 19





Jump to the decuple Begin from one number to jump to the nearest decuple, jump tens then jump remaining ones for example 37 + 25





Working with the tens and ones separately and the re- combining, works well for non-regrouping tasks e.g 37 + 25 For subtraction with regrouping children can have significant difficulties e.g. 53-17 (they try 50-10, the 3-7)

Split



**Split-jump** Split tens and ones, add/subtract tens, add first ones, jump second ones. 37 + 25 involves firstly adding 30 + 20 to make 50 then add 7 makes 57 and to add 5 first add 3 to make 60 and 2 makes 62



**Compensation** Adjusts one number to make an easier addition or subtraction, then does the calculation, and finally compensates for the initial adjustment For 37 + 25:  $40 + 25 \rightarrow 65$ ,  $65 - 3 \rightarrow 62$  and for 53 - 19:  $50 - 19 \rightarrow 31 + 3 \rightarrow 34$ 



**Transformation** change both numbers to simplify an addition or subtraction while not altering the result, 37 + 25: change 37 to 40 and 25 to 22: 40 + 22= 62 and for 53 - 19: 54 - 20 = 34



**Complementary addition or 'adding up to subtract'** used especially when the difference between the minuend and subtrahend is relatively small. This strategy is likely to arise when a missing addend task is posed such as  $39 + \Box = 50$ . For 50 - 39, jump to the decuple is very common:  $39 + 1 \rightarrow 40$ ,  $+ 10 \rightarrow 50$ , answer: 1 + 10 = 11. Commonly used for mentally calculating change in shopping transactions, this strategy is referred to as shopkeeper addition.



#### Jottings, Semi formal algorithms and formal algorithms

Writing can be used to make larger calculations more efficient and reliable. We distinguish three different kinds of written computation methods:

Jotting - for idiosyncratic informal writing to help solve a calculation problem.

Semi-formal written strategies are well-organised, standardised, usually taught written strategies.

Formal algorithms are probably the most familiar written computation methods. Algorithm means a step-by-step procedure for computing a standard task.

When children have developed competency with multi-digit mental computation, they are ready to develop written computation methods. Children are invited to try jotting, and possibly invent their own written methods.

Over time, children become familiar with the practice of using writing to support calculations.

Semi-formal strategies can be introduced, in order of simplicity: addition first, then subtraction, and later, multiplication and division.

If children are continuing to need practical resources for calculating, consider whether they are ready for written methods.

Ensure the numbers given are appropriate to the strategy being used.

#### Jottings

Jottings focus on the development of efficient mental strategies for multiplication and division in the range 1 to 100. Next encourage them to try using jottings for tasks in the range 1 to 1000. The calculations are quite complex and jotting can become very useful. They may need help in organising their jottings. Children learning to connect their own writing with their own thinking is a fundamental goal.

#### Semi formal and Notating strategies

These are well organised strategies to help keep track of the calculation. They can be personal but more usually are modelled strategies which are embedded in a student's **number sense** and involves conceptual place value. It relies on multi-digit mental calculation and the student has a sense of what the answer might be. Notating provides a record of the strategies children use to record their thinking after they have solved the task. As children describe their thinking, notate their strategies "How did you get that answer?"

#### Formal written strategies

These are referred to as *standard* or *traditional* strategies that show a step by step procedure dependent upon a precise layout. They rely on an understanding of conventional place value notation to keep track of the meaning. The final total is never conceived; instead it simply appears through the working out process.

# **Stage 1 - Early Years Foundation Stage**

# Number, Counting and Early Calculation

Although Maths is not a Prime area of the Foundation stage curriculum, as a school we are committed to ensuring children have a firm foundation in Maths to develop a secure and broad sense of Number, counting and early calculation.

Key Learning: Number	<u>40 – 60 months</u>
<u>22-36 months</u>	<ul> <li>Recognise some numerals of personal significance.</li> </ul>
Selects a small number of objects from a group when asked, for example, 'please give me	• Recognises numerals 1 to 5.
one', 'please give me two'.	• Counts up to three or four objects by saying one number name for each item.
<ul> <li>Recites some number names in sequence.</li> </ul>	<ul> <li>Counts actions or objects which cannot be moved.</li> </ul>
<ul> <li>Creates and experiments with symbols and marks representing ideas of number.</li> </ul>	<ul> <li>Counts objects to 10, and beginning to count beyond 10.</li> </ul>
<ul> <li>Begins to make comparisons between quantities.</li> </ul>	<ul> <li>Counts out up to six objects from a larger group.</li> </ul>
<ul> <li>Uses some language of quantities, such as 'more' and 'a lot'.</li> </ul>	<ul> <li>Selects the correct numeral to represent 1 to 5, then 1 to 10 objects.</li> </ul>
<ul> <li>Knows that a group of things changes in quantity when something is added or taken</li> </ul>	<ul> <li>Counts an irregular arrangement of up to ten objects.</li> </ul>
away.	<ul> <li>Estimates how many objects they can see and checks by counting them.</li> </ul>
<u>30-50 months</u>	<ul> <li>Uses the language of 'more' and 'fewer' to compare two sets of objects.</li> </ul>
<ul> <li>Uses some number names and number language spontaneously.</li> </ul>	<ul> <li>Finds the total number of items in two groups by counting all of them.</li> </ul>
<ul> <li>Uses some number names accurately in play.</li> </ul>	<ul> <li>Says the number that is one more than a given number.</li> </ul>
<ul> <li>Recites numbers in order to 10.</li> </ul>	• Finds one more or one less from a group of up to five objects, then ten objects.
<ul> <li>Knows that numbers identify how many objects are in a set.</li> </ul>	• In practical activities and discussion, beginning to use the vocabulary involved in adding
<ul> <li>Beginning to represent numbers using fingers, marks on paper or pictures.</li> </ul>	and subtracting.
<ul> <li>Sometimes matches numeral and quantity correctly.</li> </ul>	<ul> <li>Records, using marks that they can interpret and explain.</li> </ul>
<ul> <li>Shows curiosity about numbers by offering comments or asking questions.</li> </ul>	• Begins to identify own mathematical problems based on own interests and fascinations.
<ul> <li>Compares two groups of objects, saying when they have the same number.</li> </ul>	
<ul> <li>Shows an interest in number problems.</li> </ul>	
• Separates a group of three or four objects in different ways, beginning to recognise that	Early Learning Goal
the total is still the same.	Children count reliably with numbers from one to 20, place them in order and say which
<ul> <li>Shows an interest in numerals in the environment.</li> </ul>	number is one more or one less than a given number. Using quantities and objects, they
<ul> <li>Shows an interest in representing numbers.</li> </ul>	add and subtract two single-digit numbers and count on or back to find the answer. They
• Realises not only objects, but anything can be counted, including steps, claps or jumps.	solve problems, including doubling, halving and sharing.

Key Vocabualry: addition add, more, and make, sum, total altogether score double one more, two more, ten more how many more to make ? how many more is than?	Key Vocabulary: subtraction take (away), leave how many are left/left over? how many have gone? one less, two less ten less how many fewer is than? difference between is the same as
<ul> <li>Skills in early addition</li> <li>Counting all – a child doing 2 and 3 more, counts out 2 bricks and then three bricks and then finds the total by counting all the bricks.</li> <li>Counting on from the first number – a child finding 3 + 5 counts on from the first number "four, five, six, seven, eight."</li> <li>Counting on from the larger number – a child chooses the larger number, even when it is not the first number and counts on from there.</li> <li>Using a known fact – where a child gives an immediate response to facts known by heart.</li> </ul>	<ul> <li>Skills in early subtraction         Counting out – a child finding three less than 9 holds up 9 finger and folds 3 down.         Counting back from – a child finding 9 take away 3 counts back three numbers from 9, "eight, seven, six."         Counting back to – a child doing 7 – 3 counts back from the first number to the second, keeping a tally using fingers of the number of numbers that have been said, "six, five four."     </li> </ul>
Mental calculations Children must have strong number sense in order to develop early cal Haylock and Cockburn (2008) - Understanding number Cardinal aspect – matching a digit to the concrete objects, so matching the number 3 to 3 b Nominal aspect – label various items and help distinguish items e.g. 3 on a bus. Ordinal aspect – to place things in order e.g. page 3 in a book, on a clock face, flat number 3 <u>Counting</u> Pre experiences ability to categorise - to be able to identify and separate off the members of a set in order Rich experience of talk using language such as "one more" and "another one". Distinguish between small numbers before the engage in counting. Subitising. Stable order principle – repetition of saying numbers in order, it is fixed e.g. three always ca One to one principle – one number name to one object. Cardinal principle – the last number said is the number in the set. Ordinal and cardinal prin Abstraction principle – does not matter what the representation is for 3+4=7, you use the s Order irrelevance principal – whether count a row of objects forwards or backwards, it mak Conservation of number – arrangement of objects makes no difference.	ears, counters, bikes 3. that you can then count just these objects and no others. omes after 2. ciple of number come together – to label the objects and order them. same number names, in the same order, with the same one to one matching process. kes no difference.

Early addition and subtractions skills to develop
On the boil
Autumn - Counting forwards and backwards to 10 by rote.
Find a numicon shape/dice shape which is one more/one less than numbers to 10.
Count objects accurately using one to one correspondence.
Spring - Find a numicon shape/dice shape which is one more/one less than teen numbers.
Count objects accurately using one to one correspondence.
Summer - Count on and back in 1s from any number up to 20. Say the number that is 1 more/less than a given number.
Use stories, pictures, objects to solve addition and subtraction problems up to 20. Practise counting on or back to find the answer.
Early multiplication and division skills to develop
On the boil
Autumn - Sharing objects between children/toys.
Spring - Sharing objects between children/toys and checking that it is an equal share (fair).
Summer - Show doubling using fingers or objects and using 'real life' situations e.g. double the number of children in the line, insects on the leaf. Chop objects in half and use language to
describe what has happened. Half of a group of children to be inside and half to be outside.
Sharing objects between children/toys and checking that it is an equal share (fair).
<u>Visual Aids</u>
Number Tracks         2         3         8         9

# Stage 2 – Year 1 Addition and Subtraction

#### Key Learning:

- Solve problems involving counting, adding and subtracting in the context of numbers, measures or money, for example to 'pay' and 'give change'.
- Describe ways of solving puzzles and problems, explaining choices and decisions orally or using pictures.
- Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs.
- Represent and use number bonds and related subtraction facts within 20.
- Add and subtract one-digit and two-digit numbers to 20, including zero (using concrete objects and pictorial representations) Relate addition to counting on; recognise that addition can be done in any order; use practical and informal written methods to support, understand subtraction as take away, find a difference by counting up; use practical and informal methods to support the subtraction.
- Solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 =  $\Box$  9.

Key Vocabulary: +, add, more, plus numberline make, sum, total altogether score double, near double one more, two more ten more count on how many more to make? how many more is than?	Addition 8 + 3 = 11 Addend Addend Sum or Total Subtraction 8 - 3 = 5 Minuend Subtrahend Difference	-, subtract, take (away), minus Leave count back how many are left/left over? how many have gone? one less, two less, ten less how many fewer is than? how much less is? difference between half, halve
		=, equals, sign, is the same as

#### Mental calculations:

Count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number.

Count in multiples of twos, fives and tens.

Given a number, identify one more and one less for multiples of 10.

#### On the boil

Use stories, pictures, objects to build up the story of all numbers to 5/10.

Find totals by counting all.

To use the equals sign to balance sums using apparatus.

Find totals of two sets of objects by counting on.

Doubling and halving objects up to double 10.

### Addition – Add with numbers up to 20.

### Children should:

Have access to a wide range of counting equipment, everyday objects, number tracks and number lines, and be shown numbers in different contexts. Read and write the addition (+) and equals (=) signs within number sentences. Interpret addition number sentences and solve missing box problems, using concrete objects and number line addition to solve them:

8 + 3 = ? 5 + 4 = ? 5 + 3 + 1 = ? ? + ? = 6

This builds on from prior learning of adding by combining two sets of objects into one group (5 cubes and 3 cubes) in Early Years.

The four advanced counting strategies -

```
Counting on e.g. 8 + 4 = []
Counting up to e.g. 8 + [] = 12
Counting back from 12 - 4 = []
Counting back to 12 - [] = 8.
```

Use numbered number lines to add, by counting on in ones. Encourage children to start with the larger number and count on.



Numberlines, bead strings or bead bars can be used to illustrate addition, including bridging though ten by counting on 2 then on 3.

8 + 5 =



#### <u>Subtraction – Subtract from numbers up to 20.</u>



Problems should include the terms: put together, add, altogether, total, take away, distance between, difference between, more than and less than, so that pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly.

# Stage 2 – Year 2 Addition and Subtraction

#### Key Learning:

- Present solutions to puzzles and problems in an organised way; explain decisions, methods and results in pictorial, spoken or written form, using mathematical language and number sentences.
- Solve problems involving addition and subtraction, multiplication in contexts of numbers, measures or pounds and pence.
- Identify and record the information or calculation needed to solve a puzzle or problem; carry out the steps or calculations and check the solution in the context of the problem.
- Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting).
- Select a mental strategy appropriate for the numbers involved in the calculation.
- Show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot.
- Understand subtraction as take away and difference (how many more, how many less/fewer).
- Recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100.
- Recall and use number bonds for multiples of 5 totalling 60 (to support telling time to nearest 5 minutes).
- Add and subtract numbers using concrete objects, pictorial representations, and mentally, including:
  - o a two-digit number and ones (units)
  - a two-digit number and tens
  - two two-digit numbers
  - adding three one-digit numbers

Key Vocabulary:	Addition	-, subtract, subtraction, take (away), minus
+, add, addition, more, plus	8 + 3 = 11	leave, how many are left/left over?
make, sum, total, altogether	-1 1 K	one less, two less ten less one hundred less
score, double, near double	Addend Addend Sum or Total	how many fewer is than?
one more, two more ten more one	Subtraction	how much less is?
hundred more	<u>9</u> 2 - 5	difference between
how many more to make?	0-3 = 0	half, halve
how many more is than?	Mining Cubrishand Difference	= equals sign is the same as
how much more is?	Mindend Subtranend Difference	tens boundary

#### Mental calculations:

Count in steps of 2, 3, and 5 from 0, and in 10s from any number, forward and backward.

Find 1 or 10 more or less than a given number.

On the boil - Autumn	On the boil - Spring	On the boil - Summer
Recalling addition and subtraction facts to 10 and 20.	Recalling addition and subtraction facts within 20,	Recalling addition and subtraction facts within 20, represented as
Addition and subtraction of single-digit numbers,	interpreting missing number questions with = symbol in	missing number problems with = symbol in any position.
including crossing 10 by counting on/back.	any position.	Addition and subtraction of two digit and single digit numbers by
Add three single digit numbers by reordering i.e. 1 + 3	Addition and subtraction of teen numbers and single digit	reordering i.e. putting largest number first/looking for bonds.
+ 9 – putting the largest number 1 <sup>st</sup> or finding bonds.	numbers by counting on/back from the largest number.	Add several single digit numbers by reordering i.e. 3 + 3 + 8 + 2 =
Doubling and halving numbers – rapid recall up to	Add several single digit numbers by reordering i.e. 3 + 3 +	using doubles/bonds.
10+10.	8 + 2 = using doubles/bonds.	Doubling and halving numbers – rapid recall up to 20 + 20.
	Doubling and halving numbers – rapid recall up to 10 +	
	10.	



#### 

# Stage 3 – Year 3 Addition and Subtraction

#### Key Learning:

- Recall/use addition/subtraction facts for 100 (multiples of 5 and 10).
- Derive and use addition and subtraction facts for 100.
- Derive and use addition and subtraction facts for multiples of 100 totalling 1000.
- Add and subtract numbers mentally, including:
  - o a three-digit number and ones (units)
  - o a three-digit number and tens
  - o a three-digit number and hundreds
- Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction.
- Estimate the answer to a calculation and use inverse operations to check answers.
- Solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction.

<ul> <li>+, add, addition, more, plus make, sum, total altogether score double, near double one more, two more ten more one hundred more how many more to make? how many more is than? how much more is?</li> </ul>	Addend Addend Sum or Total Subtraction 8 - 3 = 5 Minuend Subtrahend Difference	-, subtract, subtraction, take (away), minus leave, how many are left/left over? one less, two less ten less one hundred less how many fewer is than? how much less is? difference between half, halve =, equals, sign, is the same as tens boundary, hundreds boundary
Mental calculations:Find 1, 10 or 100 more or less than a given number.Count up and down in tenths.On the boilRapid recall of addition and subtraction facts within 20, repressDoubling and halving numbers – rapid recall up to 20 + 20.	ented as missing number problems with = symbol in	any position.
Autumn Rapid recall of pairs of numbers totalling 5, 10 and 20.	<b>Spring</b> Use bonds to derive pairs of numbers to any multip	Summer le of Use bonds to derive pairs of numbers to any multiple of 10 or

Autumn	Spring	Summer
Rapid recall of pairs of numbers totalling 5, 10 and 20.	Use bonds to derive pairs of numbers to any multiple of	Use bonds to derive pairs of numbers to any multiple of 10 or
Bridging when adding a single digit to a two digit number. le.	10 or 100. le. 3 + 7 = 10 therefore 13 + 7 = 20 and 23 + 7	100 i.e. 3 + 7 = 10 therefore 13 + 7 = 20 and 23 + 7 = 30.
36 + 7 = 36 + 4 + 3.	= 30.	Bridging/rounding when adding a single digit number to a two
Add two/three numbers by reordering ie. 6 + 7 + 3 =.	Bridging/rounding when adding a single digit number to	or three digit number i.e. 136 + 8 = 136 + 4+ 4 or 136 + 10 -2.
	a two or three digit number ie. 136 + 8 = 136 + 4+ 4 or	Add two/three two digit numbers by reordering ie. 40 + 25 +
	136 + 10 -2.	60 + 75 =.
	Add two/three numbers by reordering ie. 6 + 7 + 3 =.	Use doubles to support understanding of 4s and 8s times
	Use doubles to support understanding of 4s and 8s times	tables.
	tables.	



# Stage 3 – Year 4 Addition and Subtraction

#### Key Learning:

- Report solutions to puzzles and problems, giving explanations and reasoning orally and in writing, using diagrams and symbols.
- Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method).
- Select a mental strategy appropriate for the numbers involved in the calculation.
- Recall and use addition and subtraction facts for 100.
- Recall and use +/- facts for multiples of 100 totalling 1000.
- Derive and use addition and subtraction facts for 1 and 10 (with decimal numbers to one decimal place).
- Add and subtract mentally combinations of two and three digit numbers and decimals to one decimal place.
- Add and subtract numbers with up to 4 digits and decimals with one decimal place using the formal written methods of columnar addition and subtraction where appropriate.
- Estimate; use inverse operations to check answers to a calculation.
- Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why.
- Solve addition and subtraction problems involving missing numbers.

Key Vocabulary:	Addition	
add, addition, more, plus, <b>increase</b> sum, total, altogether score double, near double how many more to make?	8 + 3 = 11 Addend Addend Sum or Total Subtraction 8 - 3 = 5	subtract, subtraction, take (away), minus, decrease leave, how many are left/left over? difference between half, halve how many more/fewer is than? how much more/less is?
	Minuena Subtranena Ditterence	equals, sign, is the same as tens boundary, hundreds boundary inverse

#### **Mental calculations:**

Count in multiples of 6, 7, 9, 25 and 1000.

### On the boil

Rapid recall of addition and subtraction facts within 20, represented as missing number problems with = symbol in any position. Make links to finding facts to 200, 2000 etc.,

Children practice selecting which mental calculation strategy is the most efficient when presented with different calculations i.e. round and adjust, find the difference, reorder, partition, count on, count back, doubles, near doubles, halves and bonds.

Autumn	Spring	Summer
Use bonds to derive pairs of numbers to any	Derive bonds to 1 etc from bonds to 10. le. 3 + 7 = 10 therefore 0.3 +	Derive bonds to 0.1, etc from known bonds ie. 4 + 6 = 10
multiple of 10 or 100. le. 3 + 7 = 10 therefore 13 +	0.7 = 1.	therefore 0.04 + 0.06 = 0.1.
7 = 20 and 23 + 7 = 30.		

#### Addition – Add with numbers up to 4-digit.

Move from expanded addition to the compact column method, adding units first, and 'carrying' numbers underneath the calculation. Also include money and measures contexts.

e.g. 3517 + 396 = 3913

3517 + <u>396</u> 3913 Add units first.

> 'Carry' numbers underneath the bottom line.

Introduce the compact column addition method by asking children to add the two given numbers together using the method that they are familiar with (expanded column addition—see Y3). Teacher models the compact method with carrying, asking children to discuss similarities and differences and establish how it is carried out.

Reinforce correct place value by reminding them the actual value is <u>5 hundreds</u> add <u>3 hun-</u> <u>dreds</u>, **not 5 add 3**, for example.

Use and apply this method to money and measurement values.

#### Subtraction – Subtract with up to 4-digit numbers.

#### Partitioned column subtraction with 'exchanging' (decomposition):

	2	7	5	4	1	1	5	6	2	¥	۱	١	9	2
	2	0	0	0	+	60	00	0	+	5	0	+	4	
-	1	0	0	0	+	5	0	0	+	6	0	+	2	
	1	0	0	0	1	1	0	0	+	9	0	+	2	

As introduced in V3, but moving towards more complex numbers and values. Use place value counters to reinforce 'exchanging'.

Children who are all not secure with number facts and place value will need to remain on the partitioned column method until ready for the compact method.

Compact column btraction



Give plenty of opportunities to apply this to money and measures. To introduce the compact method, ask children to perform a subtraction calculation with the familiar partitioned column subtraction then display the compact version for the calculation they have done. Ask pupils to consider how it relates to the method they know, what is similar and what is different, to develop an understanding of it (shown on video).

> Always encourage children to consider the best method for the numbers involved mental, counting on, counting back or written method (see video).

# Stage 4 – Year 5 Addition and Subtraction

#### Key Learning:

- Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method).
- Select a mental strategy appropriate for the numbers involved in the calculation.
- Recall and use addition and subtraction facts for 1 and 10 (with decimal numbers to one decimal place).
- Derive and use addition and subtraction facts for 1 (with decimal numbers to two decimal places).
- Add and subtract numbers mentally with increasingly large numbers and decimals to two decimal places.
- Add and subtract whole numbers with more than 4 digits and decimals with two decimal places, including using formal written methods (columnar addition and subtraction).
- Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy.
- Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why.
- Solve addition and subtraction problems involving missing numbers.

#### Key Vocabulary:

add, addition, more, plus, increase sum, total, altogether score double, near double how many more to make?	Addition 8 + 3 = 11 Addend Addend Sum or Total Subtraction 8 - 3 = 5	subtract, subtraction, take (away), minus, decrease leave, how many are left/left over? difference between half, halve how many more/fewer is than? how much more/less is?
	Minuend Subtrahend Difference	equals, sign, is the same as tens boundary, hundreds boundary units boundary, tenths boundary inverse

#### Mental calculations:

Count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000. Count forwards and backwards in decimal steps.

#### On the boil

Children practice selecting which mental calculation strategy is the most efficient when presented with increasingly challenging calculations i.e. round and adjust, find the difference, reorder, partition, count on, count back, doubles, near doubles, halves and bonds.

Autumn	Spring	Summer
Derive bonds to 0.1, etc from known bonds i.e. 4 + 6 =	Derive bonds to hundredths from known bonds i.e. 4 + 6 = 10	Derive as many facts as possible from bonds to 10 using
10 therefore 0.04 + 0.06 = 0.1.	therefore 0.004 + 0.006 = 0.01.	place value knowledge.



# Stage 4 – Year 6 Addition and Subtraction

#### Key Learning:

- Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method).
- Select a mental strategy appropriate for the numbers in the calculation.
- Recall and use addition and subtraction facts for 1 (with decimals to two decimal places).
- Perform mental calculations including with mixed operations and large numbers and decimals.
- Add and subtract whole numbers and decimals using formal written methods (columnar addition and subtraction).
- Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.
- Use knowledge of the order of operations to carry out calculations.
   Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why.
- Solve problems involving all four operations, including those with missing numbers.

Key Vocabulary:	Addition	subtract, subtraction, take (away), minus, decrease			
add, addition, more, plus, increase	8 + 3 = 11	leave, how many are left/left over?			
sum, total, altogether	Addend Addend Sum or Total	difference between			
score	Subtraction	half, halve			
double, near double	8 - 3 = 5	how many more/fewer is than?			
how many more to make?	Minuend Subtrahend Difference	how much more/less is?			
	Minuend Subtrahend Difference	equals, sign, is the same as tens boundary, hundreds boundary units boundary, tenths boundary inverse			

#### Mental calculations:

Count forwards or backwards in steps of integers, decimals, powers of 10.

Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method).

Select a mental strategy appropriate for the numbers in the calculation.

Recall and use addition and subtraction facts for 1 (with decimals to two decimal places).

Perform mental calculations including with mixed operations and large numbers and decimals.

# <u>On the boil</u>

Rapid recall of addition and subtraction facts within 20, represented as missing number problems with = symbol in any position. Make links to algebra i.e. 2x + 3 = 20.

Derive as many facts as possible from bonds to 10/20 using place value knowledge i.e. 120 + 80 = 200 because 12 + 8 = 20 and 3.1 + 0.9 = 4 because one tenth and nine tenths equal ten tenths or one. Make links to algebra 5 + ? = 10.6.

Children practice selecting which mental calculation strategy is the most efficient when presented with increasingly challenging calculations i.e. round and adjust, find the difference, reorder, partition, count on, count back, doubles, near doubles, halves and bonds.



# Stage 2 – Year 1 Multiplication and Division

#### Key Learning:

- Recall and use doubles of all numbers to 10 and corresponding halves.
- Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

<u>Key Vocabulary:</u> double	Multiplication 6 × 3 = 18 Factor Factor Product (or Multiplier) (or Multiplicand)		halve share left, left over
	Division 12 ÷ 3 = 4 Dividend Divisor Quotient		

#### Mental calculations:

Count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number

Count in multiples of twos, fives and tens

Recognise and create repeating patterns with numbers, objects and shapes

#### On the boil

Autumn

Grouping and sharing contexts

#### Spring and Summer

Creating arrays to explore the vocabulary around multiplication and division.

## Multiplication – Multiply with concrete objects, arrays and pictorial representations.

How many legs will 3 teddies have?



There are 3 sweets in one bag. How many sweets are in 5 bags altogether?



- Give children experience of counting equal group of objects in 2s, . 5s and 10s.
- Present practical problem solving activities involving counting equal . sets or groups, as above.

### **Division – Group and share small quantities.**

Using objects, diagrams and pictorial representations to solve problems involving both grouping and sharing.

# How many groups of 4 can be made with 12 stars? = 3



12 shared between 3 is 4

Example division problem in a familiar context:

There are 6 pupils on this table and there are 18 pieces of fruit to share between us. If we share them equally, how many will we each get?

Can they work it out and give a division statement\_? "18 shared between 6 people gives you 3 each."

# Pupils should :

- use lots of practical apparatus, arrays and picture representations ٠
- Be taught to understand the difference between 'grouping' objects (How . many groups of 2 can you make?) and 'sharing' (Share these sweets between 2 people)
- Be able to count in multiples of 2s, 5s and 10s. .
- Find half of a group of objects by sharing into 2 equal groups.

# Stage 2 – Year 2 Multiplication and Division

#### Key Learning:

- Understand multiplication as repeated addition.
- Understand division as sharing and grouping and that a division calculation can have a remainder.
- Show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot.
- Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers.
- Derive and use doubles of simple two-digit numbers (numbers in which the ones total less than 10).
- Derive and use halves of simple two-digit even numbers (numbers in which the tens are even).
- Calculate mathematical statements for multiplication using repeated addition) and division within the multiplication tables and write them using the multiplication (×), division
   (÷) and equals (=) signs.
- Solve problems involving multiplication and division (including those with remainders), using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.

Key Vocabulary: lots of, groups of ', times, multiply, multiplied by multiple of once, twice, three times ten	Multiplication 6 × 3 = 18 Factor (or Multiplier) (or Multiplicand)	halve share, share equally one each, two each, three each group in pairs, threes tens
times as (big, long, wide and so on) repeated addition array	Dividend Divisor Quotient	divide, divided by, divided into left, left over
<b>row, column</b> double		

### Mental calculations:

Count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and backward. Understand the connection between the 10 multiplication table and place value.

# On the boil

# Autumn

Rapid recall of multiplication and related division facts – 2s and 10s link to arrays and jumps along a number line.

# Spring

Rapid recall of multiplication and related division facts - 2s, 5s and 10s link to arrays and jumps along a number line.

### Summer

Rapid recall of multiplication and related division facts – 2s, 5s and 10s link to arrays and jumps along a number line.



# Stage 3 – Year 3 Multiplication and Division

#### Key Learning:

- Understand that division is the inverse of multiplication and vice versa.
- Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables.
- Derive and use doubles of all numbers to 100 and corresponding halves.
- Derive and use doubles of all multiples of 50 to 500.
- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.
- Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.
- Solve problems, including missing number problems, involving multiplication and division (and interpreting remainders), including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.

Key Vocabulary:	Multiplication					
lots of, groups of	$6 \times 3 = 18$	$6 \times 3 = 18$ halve share equally				
´, times, multiply, multiplication,						
multiplied by	Factor Factor Product	one each, two each, three each				
multiple of, <b>product</b>	(or Multiplier) (or Multiplicand)	Multiplier) (or Multiplicand) group in pairs, threes tens				
once, twice, three times ten times	Division	equal groups of ,, divide, division, divided by, divided into				
times as (big, long, wide and so on)	12 - 2 = 1 =					
repeated addition	12.3-4	left, left over, <b>remainder</b>				
array	Dividend Divisor Quotient					
row, column						
double,						
Mental calculations:						
Count from 0 in multiples of 4, 8, 50 and 100.						
Count up and down in tenths.						
Find the effect of multiplying a one- or two-d	git number by 10 and 100, identify the value	of the digits in the answer				
Summer	Autumn		Spring			
Rapid recall of multiplication and related	Rapid recall of multiplication and related	division facts – 2s, 5s and 10s.	Rapid recall of multiplication and related division facts –			
division facts – 1, 2, 3, 4, 5, 8, 50 and 100.			2s, 5s, 4s, 50s, 100s.			

![](_page_28_Figure_0.jpeg)

# Stage 3 – Year 4 Multiplication and Division

#### Key Learning:

- Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method).
- Recognise and use factor pairs and commutativity in mental calculations.
- Recall multiplication and division facts for multiplication tables up to 12 × 12.
- Use partitioning to double or halve any number, including decimals to one decimal place.
- Use place value, known and derived facts to multiply and divide mentally, including:
- multiplying by 0 and 1
- dividing by 1
- multiplying together three numbers
- Multiply two-digit and three-digit numbers by a one-digit number using formal written layout.
- Divide numbers up to 3 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.
- Use estimation and inverse to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.
- Solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, *division (including interpreting remainders),* integer scaling problems and harder correspondence problems such as n objects are connected to m objects.

Key Vocabulary:	Multiplication	
lots of, groups of times, multiply, multiplication, multiplied by multiple of, product once, twice, three times ten times times as (big, long, wide and so on) repeated addition array column double, row,	6 × 3 = 18 Factor Factor Product (or Multiplier) (or Multiplicand) Division 12 ÷ 3 = 4 Dividend Divisor Quotient	halve share, share equally one each, two each, three each group in pairs, threes tens equal groups of divide, division, divided by, divided into remainder factor, quotient, divisible by inverse

#### Mental calculations:

Count in multiples of 6, 7, 9, 25 and 1000.

On the boil - Autumn	On the boil - Spring	On the boil - Summer
Doubling and halving numbers – rapid recall up	Double and halve two and three digit numbers by partitioning.	Using double facts to double and halve tenths.
to 20 + 20.	Rapid recall of 11 and 9 times tables ( if learnt in Autumn term).	Rapid recall of all multiplication facts up to 12 x 12.
Rapid recall of multiplication and related		
division facts – 1, 2, 3, 4, 5, 8, 50 and 100.		

<u>Multiplication – Multiply 2 and 3-digits by a single digit, using all multiplication</u> tables up to 12 x 12.

# Developing the grid method

![](_page_30_Figure_2.jpeg)

Children should be able to:

Approximate before they calculate, and make this a regular part of their calculating, going back to the approximation to check the reasonableness of their answer. Eg:  $246 \times 0$  is approximately  $250 \times 10 = 2500$ 

346 x 9 is approximately 350 x 10 = 3500

Multiply multiples of ten and one hundred by a single-digit, using their multiplication to ble longuide day.

multiplication table knowledge.

Recall all times tables up to 12 x 12.

<u>Division – Divide 2 and 3 digit numbers by a single digit, with no remainders in the final answer.</u>

# 'Bus-stop' method for division

![](_page_30_Figure_11.jpeg)

Limited numbers to NO remainders in the answer or carried (each digit must be a multiple of the divisor)

\_Remind children of the correct place value, that 96 is equal to 90 and 6, but in short division, pose:

How many 3's in 9? = 3, and record it above the 9 tens. How many 3's in 6? = 2, and record it above the 6 units.

![](_page_30_Figure_15.jpeg)

Limited numbers to NO remainders in the final answer, but with remainders occurring within the calculation process.

![](_page_30_Figure_17.jpeg)

Pupils need to move onto dividing m=numbers with up to 3-digitd by a single digit, however problems and calculations provided should not result in a final answer with a remainder at this stage.

![](_page_30_Figure_19.jpeg)

When the answer for the first column is zero ( $1 \div 5$ , as an example), children could initially write a zero above to acknowledge its place, and must always 'carry' the number (1) over to the next digit as a remainder.

Real life contexts need to be used routinely to help pupils gain a full understanding, and the ability to recognise the place of division and how to apply it to problems.

# Stage 4 – Year 5 Multiplication and Division

#### Key Learning:

- Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method).
- Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.
- Know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers.
- Establish whether a number up to 100 is prime and recall prime numbers up to 19.
- Recognise and use square (<sup>2</sup>) and cube (<sup>3</sup>) numbers, and notation.
- Use partitioning to double or halve any number, including decimals to two decimal places.
- Multiply and divide numbers mentally drawing upon known facts.
- Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000.
- Solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes.
- Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers; Refine and use efficient written methods to multiply, for example HTU × U, TU × TU, U.t × U and TU.t h × TU.
- Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context; Refine and use efficient written methods to divide, for example HTU ÷U, U.t × U and HTU ÷ U.
- Use estimation/inverse to check answers to calculations; determine, in the context of a problem, an appropriate degree of accuracy.
- Solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign.
- Solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates.

Key Vocabulary:	Multiplication	
lots of, groups of	$6 \times 3 = 18$	halve
times, multiply, multiplication,		share, share equally
multiplied by	Factor Factor Product	one each, two each, three each
multiple of, product	(or Multiplier) (or Multiplicand)	group in pairs, threes tens
once, twice, three times ten times	Division	equal groups of
times as (big, long, wide and so on)	-12 - 3 = 4 =	divide, division, divided by, divided into
repeated addition		remainder
array column	Dividend Divisor Quotient	factor, quotient, divisible by
double,		inverse
row,		

### Mental calculations:

Multiply and divide numbers mentally drawing upon known facts

Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method).

On the boil – Autumn	On the boil – Spring	On the boil – Summer
Use key vocabulary – sum, product, difference – to practice	Use key vocabulary – sum, product, difference, square, cube	Use key vocabulary – sum, product, difference, square, cube
finding the sum, product difference of two single digit	to practice finding the sum, product, difference, square and	to practice finding the sum, product, difference, square and
numbers.	cube of given numbers.	cube of given numbers.
Rapid recall of all multiplication facts up to 12 x 12.	Rapid recall of known factors within children's'	Identify prime numbers within a given range and square
	multiplication facts.	numbers up to 144.

#### Multiplication – Multiply up to 4-digits by 1 or 2 digits.

### **Column Multiplication**

Introduce by comparing a grid method calculation to a short mulitplication method, to see how the steps are related, but notice how there are less steps involved in the column method.

Chidlren need to be taugthj to approximate first, e.g. for 72 x 38, they will use rounding: 72 x 38 is approximately 70 x 40 = 2800, and use this approximation to check the reasonableness of their answer against.

### Short muliplication for multiplying by a single digit

![](_page_32_Figure_5.jpeg)

Pupils could be asked to work out a given calculation using the grid method, and then compare it to 'your' column method. What are the similarities and differences? Unpick the steps and show how it reduces the steps.

### Introduce long multiplication for multiplying by 2 digits

![](_page_32_Figure_8.jpeg)

Division – Divide up to 4 digits by a single digit, including those with reminders.

Short division using the bus-stop method, including remainders in the final answer.

![](_page_32_Picture_11.jpeg)

Now that pupils are introduced to examples that give rise to remainder answers, division needs to have a real life problem solving context, where pupils consider the meaning of the remainder and how to express it. i.e. as a fraction, decimal, or as a rounded number or value depending upon the context of the problem.

The answer to 5309 ÷ 8 could be expressed as 663 and five eighths, 663 r 5, as a decimal or rounded as appropriate to the problem involved.

# Stage 4 – Year 6 Multiplication and Division

#### Key Learning:

- Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method).
- Identify common factors, common multiples and prime numbers.
- Use partitioning to double or halve any number.
- Perform mental calculations, including with mixed operations and large numbers.
- Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication.
- Multiply one-digit numbers with up to two decimal places by whole numbers.
- Divide numbers up to 4 digits by a two-digit whole number using the formal written methods of short or long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.
- Use written division methods in cases where the answer has up to two decimal places.
- Use estimation and inverse to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy. Use knowledge of the order of operations to carry out calculations.
- Solve problems involving all four operations, including those with missing numbers.

Key Vocabulary:	Multiplication	
lots of, groups of	$6 \times 3 = 18$	halve
times, multiply, multiplication,		share, share equally
multiplied by	Factor Factor Product	one each, two each, three each
multiple of, product	(or Multiplier) (or Multiplicand)	group in pairs, threes tens
once, twice, three times ten times	Division	equal groups of
times as (big, long, wide and so on)	-12 - 3 = 4 =	divide, division, divided by, divided into
repeated addition		remainder
array column	Dividend Divisor Quotient	factor, quotient, divisible by
double,		inverse
row,		

#### Mental calculations:

Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method) Perform mental calculations, including with mixed operations and large numbers

Use key vocabulary – sum, product, difference, square, cube to practice finding the sum, product, difference, square and cube of given numbers.

On the boil – Autumn	On the boil – Spring	On the boil – Summer
- Rapid recall of all multiplication facts up to 12	<ul> <li>Rapid recall of known factors within children's' multiplication</li> </ul>	
x 12 and their relevant division facts	facts.	
	- Deriving common factors for appropriate numbers	

<u>Multiplication – Short and long multiplication, with more complex numbers and</u> <u>multiply decimals with up to 2d.p by a single digit.</u>

### Long mutliplication for more complex numbers

![](_page_34_Figure_2.jpeg)

Q

7

3

Ъ

L

2

Children will be able to:

Use rounding and place value to make approximations before calculating and use these to check answers against.

Use short multiplication to multiply numbers with more than 4-digits by a single digit; to multiply money and measures, and to multiply decimals

with up to 2.d.p. by a single digit. Use long multiplication to multiply numbers with at least 4 digits by a 2-digit number.

> This works well for multiplying money (£.p) and other measures.

#### Division – Divide at least 4 digits by both single- digit and 2-digit numbers.

Short division with remainders: Pupils should continue to use this method, but with numbers to at least 4 digits, and understand how to express remainders as a fraction, decimal, whole number remainders or rounded numbers. Real life problems solving contexts need to be the starting point, where pupils have to consider the most appropriate way to express the remainder.

Short division, for dividing by a single digit:

e.g. 4697 ÷ 8 =

Line up the decimal points in the question and the answer.

Calculating a decimal remainder: In this example, rather than expressing the remainder as r. 1 a decimal point is added after the units because there is still a remainder, and the one remainder is carried onto zeros after the decimal point (to show there was no decimal value in the original number). Keep dividing to an appropriate degree of accuracy for the problem being solved.

### Introduce long division by chunking for dividing by 2 digits

![](_page_34_Figure_15.jpeg)

Where remainders occur, pupils should express them as fractions, decimals or use rounding, depending upon the problem. The following page is produced by the DFE and outline possible methods for the 4 operations. Our policy follows these guidelines and teaches pupils the steps leading up to these efficient methods.

# **Addition and subtraction**

789 +	642	beco	omes	874 – 523 becomes			ome	932 – 457 becomes	
+	7 6	8 4	9 2	_	8 5	7 2	4 3		<sup>8</sup> <sup>12</sup> <sup>1</sup> 9 <b>3</b> 2 - 4 5 7
1	<b>4</b>	<b>3</b>	1		3	5	1		4 7 5
An	swe	r: 14	31	A	nsw	ver: 3	351		Answer: 475

# Short multiplication

24 × 6 becomes	342 × 7 becomes	$2741 \times 6$ becomes	24 × 16 becomes	124 × 26 becomes	124 × 26 becomes
2 4 × 6 1 4 4 2 Answer: 144	3     4     2       ×     7       2     3     9     4       2     1   Answer: 2394	2     7     4     1       ×     6       1     6     4     4     6       4     2       Answer:     16     446	$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
			Answer: 384	Answer: 3224	Answer: 3224
Short Division			Long Division		
98 ÷ 7 becomes	432 ÷ 5 becomes	496 ÷ 11 becomes	432 ÷ 15 becomes	432 ÷ 15 becomes	432 ÷ 15 becomes
<b>1 4</b> <b>7 9 8</b> Answer: 14	<b>8 6 r 2</b> <b>5 4 3 2</b> Answer: 86 remainder 2	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	2 8 r 12 1 5 4 3 2 3 0 0 1 3 2 1 2 0 1 2	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
				$\frac{12}{15} = \frac{4}{5}$	
			Answer: 28 remainder 12	Answer: 28 <sup>4</sup> / <sub>5</sub>	Answer: 28.8

**Long Multiplication**